

2/3/2009

Two types of Data

1. Variable - takes on more than one value, variable values
2. constant - takes on only one constant = does not change

- Point Estimation - estimate the value of a particular value
- Examining Relationships - one variable is related or correlated with another. Example: x is related to y

Negative slope down

can have two variables that don't covary

Causal relationship -

- Independent variable - the cause
 - dependent variable - the effect
- Covariation - change in response to one temporal operation

Time ordering - cause of y must

come first. Ex: Gender and Delinquency

Age \rightarrow Delinquency, Grades in School \rightarrow Delinquency

NON SPURIOUSNESS

In order for X to cause Y we need to eliminate other possible of Y we need to make sure that we do not confuse other things that happen before Y.

Levels of Measurement

- Nominal - Gender
- Ordinal 15-20-21-25
- Interval = absolutely 0 Age
- Ratio = rate frequency

Frequency - List of values of data and the # of times it appears

Frequency Distribution - full range of values and # of times it occurs

Rate ~~F/population~~ ~~standard unit~~
Rate = $F / \text{population} \times \text{per } 100,000$ ^{standard unit}

standard times size X by 12

proportion divide frequency ^{# of cases}
multiply by 100 to get %

4/8/2009

difference between difference
Between 2 intervals is the same
interval ratio.

Proportion $(\frac{x}{n} \times 100)$

Percent change
 $(\text{ending value} - \text{starting value})$

1980 1,241 per 100,000
1990 1,789 per 100,000
2000 1,137 per 100,000

$(\text{ending value} - \text{starting value}) / \text{starting value} \times 100$

$1,789 - 1,241 = 548 \div 1,241 = .442$

100×44.2

~~1,137 - 1,789~~

= decrease

Number of Bad Arrest from a sample of 30 police officers

person# 1	2	0
person# 2	4	0
	6	1
	7	0
	13	0
	7	0
	10	0
	8	0
	7	0
	0	0
4		

Person# 156

CF = cumulative frequency ^{start at top} work by adding down

% vector multiply by 100

0-4 range value (class interval)

Grouped frequency distribution

Class interval = mutually exclusive
Fall into 1 and only one category

2. Make your class intervals exhaustive
3. Make your intervals all the same width.
4. Make sure that for your first class interval contains the smallest value + the last interval the highest.

Step 1 determine the number of class intervals you want

Step 2 subtract high 89 to low 22 = 67.

8. Take the ratio of the range

$$67/8 = 8.375 = 8$$

Class interval width of 8.

20 Lower interval width

~~20 - 28~~

$$20 - 27$$

$$27 - 35$$

$$36 -$$

Nominal 3 Ordinal Level data
Pie chart
Bar chart

19.5-27.5, 27.5-37.5 \neq continuous

Real class - not mutually exclusive

midpoint = exact mode of every class interval

$$m_i = \frac{LL + UL}{2} \quad \frac{\text{Lower Limit} + \text{Upper Limit}}{2}$$

$$\frac{83.5 - 91.5}{2} = 87.5$$

Mode, median, mean
highest

Dimodal = two modes
Trimodal = 3 modes

Median: interval/ratio level
50% percentile

1. Rank order the data

Find the score(s) that is in the median with formula

$$X(\text{median}) = \frac{(n+1)}{2}$$

$$X = L + \left[\frac{\frac{n+1}{2} - F}{f} \right] w_i$$

$$43.5 + \left[\frac{36+1}{2} - 0 \right] \cdot 10$$

$$43.5 + (9) \cdot 10 = 43.5 + 90 = 133.5$$

2 not give you the value of median but the position of the median

$$43.5 + \left[\frac{100+1}{2} - 36 \right] \cdot 10$$



mean:

$$\bar{X} = \frac{\sum_{i=1}^n x_i}{N}$$

Advantages = we use all our information

The distance from the mean deviation.

$$s = \sqrt{\frac{\sum (x - \bar{x})^2}{n-1}}$$

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$x = \sqrt{x^2}$ = standard deviation of
 the data. To the square of the
 the variance. The standard
 deviation is the square root
 to the variance.

Sum $x = \sqrt{\frac{10}{101}} = \sqrt{\frac{10}{9} = 1.1111}$
 1.1111 variance

Take each score subtract the mean
 squared each deviation
 the sum overall variance.

Subtract
 each score
 square
 the sum
 to get
 the sum

$$s = \sqrt{\frac{\sum(x^2) - (\sum x)^2}{n-1}}$$

$$s^2 = \frac{\sum(x^2) - \frac{(\sum x)^2}{n}}{n-1}$$

\uparrow $x_1^2 + x_2^2 + x_3^2$ \uparrow $(x_1 + x_2 + x_3)^2$

rect of x^2 sums

sum

$$\frac{170 - 40^2}{10} = 4$$

$$\frac{170 - \left(\frac{40^2}{10}\right)}{10-1}$$

$$s^2 = \frac{\sum (x_i - \bar{x})^2}{n-1}$$

NOTATION

- Subtract the mean from each value and square
- Square the deviation
- Multiply the squared deviation by the frequency and sum across all intervals
- Square

Nominal Ordinal

- Mode
- Median
- Mean
- Variance Ratio
- Interquartile Range
- Variance
- Standard deviation

$$VR = 1 - \frac{F_{mode}}{n}$$

	F
Small (50-4)	20
Medium (8-9)	50
Large (100)	150
Super Large (15)	170

$$1 - \frac{90}{170} = 1 - 0.53 = 0.47$$

NS F
 small 5.0
 Medium 2.0
 Large 2.0
 type 100 ← Mode

170

1-100

$$1 - .59 = .41\%$$

	X	F	p	%	C%
	10	6	.06	6%	6%
	11	4	.07	7%	13%
	12	9	.09	9%	22%
Q3	13	25	.25 X	25%	47%
	14	23	.23 X	23%	70%
Q1	15	14	.14	14%	84%
	16	6	.06	6%	90%
	17	3	.03	3%	93%
	18	1	.01	1%	100%
		<u>n = 100</u>	<u>1</u>	100	

CF
 6
 13
 22
 47
 70
 84
 90
 93

$$\frac{50+1}{2} = 25.5$$

Number of Rooms

1	0	0
2	2	4
3	3	9
4	4	16
5	1	1
6	1	1
7	3	9

$n=7$ 40

Mean $\frac{14}{7} = 2$

$$S = \frac{\sqrt{\sum (Ex)^2 - \frac{(Ex)^2}{n}}}{n-1} = \frac{40 - \frac{(14)^2}{7}}{6}$$

$$\sqrt{40 - \frac{196}{7}}$$

$$\sqrt{\frac{40 - 28}{6}}$$

$$\frac{12}{6} = \sqrt{2}$$

$12 = 1.41$
 $\sqrt{2} = 2$

$$s = \sqrt{\frac{\sum Fm^2 - (\sum Fm)^2}{n}}$$

$M_i + \frac{LL+UL}{2}$	F	Mi	M_i^2	Fm^2
0-4	6	2	4	24
5-9	11	7	49	39
10-14	27	12	144	324
15-19	4	17	289	156
	<u>48</u>			<u>5607</u>

Fm:

12
77
324

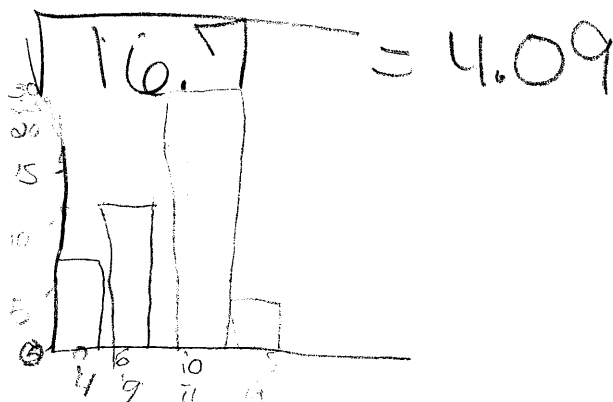
$$\frac{606}{48} = 48 = \text{meq. n}$$

$$\frac{5607 - (481)^2}{48}$$

$$48 - 1$$

$$\frac{5607 - 4820}{47}$$

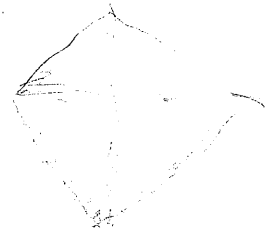
Independent variable
course
depository
etc.



$$s = \sqrt{16.7}$$

$$s = 4.09$$

$$s^2 = 16.7$$



- descriptive research answers questions
- Exploratory research to identify causes and essences of phenomena
- Evaluation research effectiveness of social programs and policy

Validity
- internal validity
- external validity
- case control

Cohort/retrospective studies
correlation studies
and case-control studies
B.

Generalizability - it is used to infer about the whole place or event from a sample
Not needed
- generalization assumes that you find a sample that is like the population from which the sample was drawn

Sampling error is the difference between the characteristics of a sample and the characteristics of the population from which it was taken.

probability sampling - All elements of a population have an equal chance of being selected. It is that any element of a population will be selected.

nonprobability sampling - methods or sampling methods that do not let us know the likelihood of being selected.

Simple random sample - generalize information to data from the sample to a larger population.

$$\text{Rate} = \frac{\text{Number in class}}{\text{Total number}} \times 100\%$$

$$\text{Proportion} = \frac{\text{Number in subset of sample}}{\text{Total number in sample}}$$

$$\text{Percent} = \text{Proportion} \times 100$$

	F	Proportion	%
\$100,000	16	0.08	8.0
\$20,000	30	0.15	15.0
\$30,000	48	0.24	24.0
\$40,000	8	0.04	4.0
\$50,000	10	0.05	5.0
\$100,000	20	0.10	10.0

Mode = highest frequency
then subtract that by 1

to find range of the data NOT
the difference between the highest and lowest

RANGE = highest - lowest

Subtract the mean from each score
then square

- Square each of these
- Add up all the squares and divide by the number of scores
- Take the square root of this
- Standard deviation
- This is the standard deviation of the scores

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• Square each of the readings
of the clock.

• Multiply each square by the
by the length of the time
interval

• Sum all the above results

• Sum all the above results
to get the total sum

• Divide the total sum by the
number of observations

• Divide the result by the
number of observations

Probability
• chance of an event occurring.

$$P(\text{H in one flip of a coin}) = .5$$

Suppose we flip a coin 10 times
10 times does it mean we are
going to get 5 heads and
5 tails? NO

expected value property of event
occurring x number of events

~~Probability~~

$$2 \times 20 = 4$$

$$P(A) = \frac{1}{n}$$

~~Probability~~

Complement of an event

The complement of event $(A) = 1 - P(A)$

Odds of an event = Ratio of an event

$$\text{odds}(A) = \frac{P(A)}{1 - P(A)}$$

Mutually Exclusive - 2 zero
probability that they can
occur together or at the
same time.

Two rules

The Bounding Rule
probabilities are bounded
by 0 and 1.0. They can never
be less than 0 or greater than 1.0.

Rule 2: The addition rule
Restricted Addition rule
only if events are mutually
exclusive

$P(A \text{ and } B)$ is the probability
of events A & B occurring together -
their joint probability.
non mutually
exclusive

$$P(A \text{ or } B) = P(A) + P(B) - P(A \text{ and } B)$$

Rule 3 multiplication Rule
 Restricted Multiplication
 rule for independent Rule.

If two events are independent
 events then the probability

Independent of
 $P(A) = P(A|B)$

$P(A)$ is the unconditional
 probability of A.

New Term: $P(A|B)$ Probability

Outcome of Trial	Retained Council	Public Defender	total
Acquitted	75	75	150
convicted	30	30	60
total	105	105	210

conditional = unconditional

	Retained Counsel	Public Defender	Total
Acquit	55	95	150
Convict	50	10	60
Total	105	105	210

If $P(A) \neq P(A|B)$ is true then the events are not independent and Rule 3a does not apply. Rule 3b applies

Rule 3b: the general Multiplication Rule of two events

Probability distribution is a theoretical distribution. It is not a distribution. It is not a distribution

$$P(0 \text{ heads}) = P(T.T.T.T) = .5 \cdot .5 \cdot .5 \cdot .5 = (.5)^4 = .0625$$

$$P(1 \text{ head}) = P(H.T.T.T) = .5 \cdot .5 \cdot .5 \cdot .5 = (.5)^4 = .0625$$

Quiz Thursday, calculate getting 2, 3, 4 heads

$$P(r) = p^r q^{n-r}$$

p
probability
event occurring

q
probability of
not occurring

$$p^r q^{n-r}$$

$$\binom{n}{r} = \frac{n!}{r!(n-r)!}$$

$$P(r) = \binom{n}{r} p^r q^{n-r}$$

$$P(r) = \left(\frac{n!}{r!(n-r)!} \right) p^r q^{n-r}$$

H_0 = null hypothesis
 H_0 = assumption of innocence

Non directional = Alternative hypothesis
which means.

A hypothesis test begins with a null and alternative hypothesis.
Let's go with a directional hypothesis.

$$P(r) = \binom{n}{r} p^r q^{n-r}$$

$$p = 0.4$$

$$q = 1 - 0.4 = 0.6$$

$$r = 0, 1, 2, 3, 4, 5$$

$$n = 5$$

mean = $n \cdot p$ of binomial distribution

5 steps

1. State the null and the alternative hypothesis
2. Select probability distribution
Binomial if 2 categories (Nominal distribution if continuous)

3. Select Alpha Level of significance
 Balance Type I (False positive)
 and Type II (False negative) Errors
 $\alpha = .05$ (.10, .05, .001)

4. Calculate the probability of observing 8 or more of 10 deaths

$$P(X) = \binom{n}{r} p^r q^{n-r} = P(8) \binom{10}{8} \left(\frac{10!}{8!(10-8)!}\right) \cdot 4^8 \cdot 6^{10-8}$$

Critical region defines the class of outcomes

Step 1 - State your hypothesis

$$D > .06$$

~~Choose Probability distribution~~ Choose probability distribution

$$\alpha = .01 \quad \alpha = .05 \quad \alpha = .001$$

Normal Normal distribution
 - Common distribution for continuous data